

Okanagan College Math 122 (071) Winter 2012 **Term Test Two**

Instructor: Jason Schaad Wednesday, February 15

Student Name:	KEY	Total Marks:	
		38	

Instructions. Do all parts of all 11 questions. Show all work and give explanations where required. You may receive part marks for a question if your work is correct even if the final answer is incorrect. However, if your answer is incorrect and no work or explanation is given, you will receive no marks. The number of points for each question is given in the left margin, total 38. A Formula Sheet is attached. You may use any of the formulas from this sheet. If you use an integral formula from the sheet, give the number of the formula that you used.

[2] 1. Evaluate
$$\int \frac{x}{1+x^2} dx$$
.

$$du = 2xdx$$

[3] 2. Evaluate
$$\int_0^1 \sin\left(\frac{\pi}{2}t\right) dt$$
.

[2] 3. Evaluate
$$\int x \sin(x) dx$$
.

$$U=X$$
 $dv=sinx dx$
 $du=dx$ $V=-cosx$

$$\int \frac{x}{1+x^2} dx = \frac{1}{2} \int \frac{dy}{y} = \frac{1}{2} |h|u| + C$$

$$=\frac{1}{2}\ln(1+x^2)+C=\frac{1}{2}\ln(1+x^2)+C$$

t=0=7U=0
$$\int \sin \frac{\pi}{k} t dt$$

t=1=7U= $\frac{\pi}{k}$ $\int \sin \frac{\pi}{k} t dt$
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$$=\frac{2}{\pi}\int_{0}^{\pi}\int_{0}^{\pi}\sin u du$$

$$= -\frac{2}{\pi} \cos u \Big|_{0}^{\pi/2} = \frac{2}{\pi} \Big[\cos(\pi/2) - \cos(0) \Big]$$

$$= \frac{2}{\pi} \Big[\cos(\pi/2) - \cos(0) \Big]$$

$$\int x \sin(x) dx = x(-\cos x) - \int (-\cos x) dx = -x \cos x + \int \cos x dx$$

$$= \left[-x \cos x + \sin x + C \right]$$

(a) Evaluate the indefinite integral $\int x \ln x \, dx$.

$$u = \ln x$$
 $dv = x dx$
 $du = \frac{1}{2}x^2$

then
$$\int x \ln x \, dx = \frac{1}{2} x^2 \ln x - \int (\frac{1}{2} x^2) (\frac{1}{2} dx)$$

 $-\frac{1}{2} x^2 \ln x - \frac{1}{2} \int x \, dx$
 $=\frac{1}{2} x^2 \ln x - \frac{1}{4} x^2 + C$
 $=\frac{1}{4} x^2 (2 \ln x - 1) + C$

(b) Evaluate the indefinite integral $\int \frac{\ln x}{x} dx$. [2]

Substitution

$$u = \ln x$$

$$du = \frac{1}{x} dx$$

then
$$\int \frac{\ln x}{x} dx = \int 4 dx = \frac{1}{2} (2 + c) = \frac{1}{2} (2 + c)$$